

## Curriculum Vitae

Neil Hindman  
Professor Emeritus  
Department of Mathematics  
Howard University  
Washington, DC 20059

**EDUCATION:**

B.A.	1965	Westmar College
M.A.	1967	University of Massachusetts
Ph.D.	1969	Wesleyan University (Dissertation <i>On <math>P</math>-like spaces and their product with <math>P</math>-spaces</i> written under the direction of W. W. Comfort.)

### PROFESSIONAL EXPERIENCE:

January 1980	– June 2017	Associate Professor and Professor, Howard University
September 1970	–December 1979	Assistant Professor, Associate Professor and Professor, California State University, Los Angeles (Except September 1975 – August 1976, Visiting Associate Professor, SUNY at Binghamton)
September 1969	–June 1970	Visiting Assistant Professor, Wesleyan University

### RESEARCH PUBLICATIONS:

(With W. Comfort and S. Negrepointis)  *$F'$ -spaces and their product with  $P$ -spaces*, Pacific J. Math. **28** (1969), 489-502. (MR **39** #3440)

*On the existence of  $\mathfrak{c}$ -points in  $\beta\mathbb{N}\setminus\mathbb{N}$* , Proc. Amer. Math. Soc. **21** (1969), 277-280. (MR **39** #922)

*Minimal  $n$ -prime ideal spaces*, Math. Ann. **199** (1972), 97-114. (MR **38** #291)

*The existence of certain ultrafilters on  $\mathbb{N}$  and a conjecture of Graham and Rothschild*, Proc. Amer. Math. Soc. **36** (1972), 341-346. (MR **46** #7041)

*Basically bounded sets and a generalized Heine–Borel Theorem*, Amer. Math. Monthly **80** (1973), 549-552. (MR **48** #3000)

*Preimages of points under the natural map from  $\beta(\mathbb{N} \times \mathbb{N})$  to  $\beta\mathbb{N} \times \beta\mathbb{N}$* , Proc. Amer. Math. Soc. **37** (1973), 603-608. (MR **50** #11154)

*The product of  $F$ -spaces with  $P$ -spaces*, Pacific J. Math. **47** (1973), 473-480. (MR **48** #9643)

- Finite sums from sequences within cells of a partition of  $\mathbb{N}$* , J. Comb. Theory (Series A) **17** (1974), 1-11. (MR **50** #2067)
- (With M. Cates) *Partition theorems for subspaces of vector spaces*, J. Comb. Theory (Series A) **19** (1975), 13-25. (MR **52** #112)
- (With M. Cates, P. Erdős, and B. Rothschild) *Partition theorems for subsets of vector spaces*, J. Comb. Theory (Series A) **20** (1976), 279-291. (MR **53** #10583)
- (With W. Comfort) *Refining families for ultrafilters*, Math. Zeit. **149** (1976), 189-199. (MR **55** #285)
- Partitions and sums of integers with repetition*, J. Comb. Theory (Series A) **27** (1979), 19-32. (MR 81b:05018)
- Partitions and sums and products of integers*, Trans. Amer. Math. Soc. **247** (1979), 227-245. (MR 80b:10022)
- Simultaneous idempotents in  $\beta\mathbb{N}\setminus\mathbb{N}$  and finite sums and products in  $\mathbb{N}$* , Proc. Amer. Math. Soc. **77** (1979), 150-154. (MR 80f:05005)
- Ultrafilters and combinatorial number theory*, in Number Theory Carbondale 1979, M. Nathanson ed., Lecture Notes in Math. **751** (1979), 119-184. (MR 81m:10019)
- Partitions and sums and products – two counterexamples*, J. Comb. Theory (Series A) **29** (1980), 113-120. (MR 82b:05020)
- Sums equal to products in  $\beta\mathbb{N}$* , Semigroup Forum **21** (1980), 221-255. (MR 81m:54040)
- On a conjecture of Erdős, Faber and Lovasz about  $n$ -colorings*, Canadian J. Math. **33** (1981), 563-570. (MR 82j:05058)
- Minimal ideals and cancellation in  $\beta\mathbb{N}$* , Semigroup Forum **25** (1982), 291-310. (MR 83m:22007)
- On density, translates, and pairwise sums of integers*, J. Comb. Theory (Series A) **33** (1982), 147-157. (MR 84b:10075)
- (With P. Erdős) *Enumeration of intersecting families*, Discrete Math. **48** (1984), 61-65. (MR 84b:10075)
- Partitions and pairwise sums and products*, J. Comb. Theory (Series A) **37** (1984), 46-60. (MR 85g:05019)
- (With J. Berglund) *Filters and the weak almost periodic compactification of a discrete semigroup*, Trans. Amer. Math. Soc. **284** (1984), 1-38. (MR 85e:22005)
- (With P. Milnes) *The ideal structure of  $X^X$* , Semigroup Forum **30** (1984), 41-51. (MR 85i:22004)
- (With J. Pym) *Free groups and semigroups in  $\beta\mathbb{N}$* , Semigroup Forum **30** (1984), 177-193. (MR 86c:22002)

- Ramsey's Theorem for sums, products, and arithmetic progressions*, J. Comb. Theory (Series A) **38** (1985), 82-83. (MR 86c:05024)
- The minimal ideals of a multiplicative and additive subsemigroup of  $\beta\mathbb{N}$* , Semigroup Forum **32** (1985), 283-292. (MR 87g:20106)
- The ideal structure of the space of  $\kappa$ -uniform ultrafilters on a discrete semigroup*, Rocky Mountain J. Math. **16** (1986), 685-701. (MR 88d:54031)
- Summable ultrafilters and finite sums*, in Logic and Combinatorics, S. Simpson ed., Contemporary Mathematics **65** (1987), 263-274. (MR 88h:03070)
- (With W. Deuber) *Partitions and sums of  $(m,p,c)$ -sets*, J. Comb. Theory (Series A) **45** (1987), 300-302. (MR 89a:05013)
- (With A. Blass) *On strongly summable ultrafilters and union ultrafilters*, Trans. Amer. Math. Soc. **304** (1987), 83-99. (MR 88i:03080)
- (With D. Davenport) *Subprincipal closed ideals in  $\beta\mathbb{N}$* , Semigroup Forum **36** (1987), 223-245. (MR 89h:54031)
- Some equivalents of the Erdős sum of reciprocals conjecture*, European J. Comb. **9** (1988), 39-47. (MR 89j:11007)
- (With P. Milnes) *The  $\mathcal{LMC}$ -compactification of a topologized semigroup*, Czechoslovak Math. J. **38** (1988), 103-119. (MR 89c:22008)
- (With V. Bergelson) *Density versions of two generalizations of Schur's Theorem*, J. Comb. Theory (Series A) **48** (1988), 32-38. (MR 90b:05017)
- (With V. Bergelson) *A combinatorially large cell of a partition of  $\mathbb{N}$* , J. Comb. Theory (Series A) **48** (1988), 39-52. (MR 89m:04003)
- Is there a point of  $\omega^*$  that sees all others?* Proc. Amer. Math. Soc. **104** (1988), 1235-1238. (MR 89d:04008)
- Solving equations in  $\beta\mathbb{N}$* , Annals N. Y. Acad. Sci. **552** (1989), 69-73. (MR 90m:54036)
- (With V. Bergelson) *Ultrafilters and multidimensional Ramsey theorems*, Combinatorica **9** (1989), 1-7. (MR 91f: 03101)
- Ultrafilters and Ramsey Theory – an update*, in Set Theory and its Applications, J. Steprāns and S. Watson eds., Lecture Notes in Math. **1401** (1989), 97-118. (MR 91f:03101)
- (With V. Bergelson, H. Furstenberg, and Y. Katznelson) *An algebraic proof of van der Waerden's Theorem*, L'enseignement Mathématique **35** (1989), 209-215. (MR 91g:11010)
- (With A. Blass) *Sums of ultrafilters and the Rudin-Keisler and Rudin-Frolík orders*, in General Topology and Applications, R. Shortt ed., Lecture Notes in Pure and Applied Math. **123** (1990), 59-70. (MR 91i:03093)

*On creating sets with large lower density*, Discrete Math. **80** (1990), 153-157. (MR 91k:28002)

(With V. Bergelson) *Nonmetrizable topological dynamics and Ramsey Theory*, Trans. Amer. Math. Soc. **320** (1990), 293-320. (MR 90k:03046)

*The semigroup  $\beta\mathbb{N}$  and its applications to number theory*, in The Analytical and Topological Theory of Semigroups – Trends and Developments, K. Hofmann, J. Lawson, and J. Pym eds., de Gruyter Expositions in Math. **1** (1990), 347-360.

(With A. Lisan) *Does  $\mathbb{N}^*$  contain a topological and algebraic copy of  $\beta\mathbb{N}$ ?* Topology and its Applications **35** (1990), 291-297. (MR 91h:54026)

*Strongly summable ultrafilters on  $\mathbb{N}$  and small maximal subgroups of  $\beta\mathbb{N}$* , Semigroup Forum **42** (1991), 63-75. (MR 92a:54025)

(With J. Pym) *Closures of singly generated subsemigroups of  $\beta S$* , Semigroup Forum **42** (1991), 147-154. (MR 92a:22004)

(With D. Davenport) *A proof of van Douwen's right ideal theorem*, Proc. Amer. Math. Soc. **113** (1991), 573-580. (MR 92f:54025)

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(With J. Berglund) *Sums of idempotents in  $\beta\mathbb{N}$* , Semigroup Forum **44** (1992), 107-111. (MR 92k:54027)

(With V. Bergelson) *Ramsey Theory in non-commutative semigroups*, Trans. Amer. Math. Soc. **330** (1992), 433-446. (MR 93j:03025)

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(With J. Baker and J. Pym) *Elements of finite order in Stone-Čech compactifications*, Proc. Edinburgh Math. Soc. **36** (1993), 49-54. (MR 93m:22003)

(With H. Lefmann) *Partition regularity of  $(\mathcal{M}, \mathcal{P}, \mathcal{C})$ -systems*, J. Comb. Theory (Series A) **64** (1993), 1-9. (MR 95b:05016)

(With W. Woan) *Central sets in semigroups and partition regularity of systems of linear equations*, Mathematika **40** (1993), 169-186. (MR 95d:20105)

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(With V. Bergelson) *Additive and multiplicative Ramsey Theorems in  $\mathbb{N}$  – some elementary results*, Comb. Prob. and Comp. **2** (1993), 221-241. (MR 95b:05208)

(With I. Leader) *Image partition regularity of matrices*, Comb. Prob. and Comp. **2** (1993), 437-463. (MR 95j:05167)

(With V. Bergelson, W. Deuber, and H. Lefmann) *Rado's Theorem for commutative rings*, J. Comb. Theory (Series A) **66** (1994), 68-92. (MR 95f:05011)

(With V. Bergelson and A. Blass) *Partition theorems for spaces of variable words*, Proc. London Math. Soc. **68** (1994), 449-476. (MR 95i:05107)

(With A. Lisan) *Points very close to the smallest ideal of  $\beta S$* , Semigroup Forum **49** (1994), 137-141. (MR 95c:22005)

(With J. Lawson and A. Lisan) *Separating points of  $\beta\mathbb{N}$  by minimal flows*, Canadian J. Math. **46** (1994), 758-771. (MR 95e:22010)

(With D. Strauss) *Cancellation in the Stone-Čech compactification of a discrete semigroup*, Proc. Edinburgh Math. Soc. **37** (1994), 379-397. (MR 95j:22006)

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(With D. Strauss) *Nearly prime subsemigroups of  $\beta\mathbb{N}$* , Semigroup Forum **51** (1995), 299-318. (MR 96k:54038)

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(With D. Strauss) *Prime properties of the smallest ideal of  $\beta\mathbb{N}$* , Semigroup Forum **52** (1996), 357-364. (MR 97c:54033)

(With V. Bergelson and B. Kra) *Iterated spectra of numbers – elementary, dynamical and algebraic approaches*, Trans. Amer. Math. Soc. **348** (1996), 893-912. (MR 97b:03058)

- (With D. Strauss) *Compact subsemigroups of  $(\beta\mathbb{N}, +)$  containing the idempotents*, Proc. Edinburgh Math. Soc. **39** (1996), 291-307. (MR 97h:22002)
- (With A. Maleki and D. Strauss) *Central sets and their combinatorial characterization*, J. Comb. Theory (Series A) **74** (1996), 188-208. (MR 98d:22002)
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- Algebra in  $\beta S$  and its applications to Ramsey Theory*, Math. Japonica **44** (1996), 581-625. (MR 97k:03059)
- (With V. Bergelson)  *$IP^*$  sets in product spaces* in Papers on General Topology and Applications, S. Andima et. al. eds., Annals of the New York Academy of Sciences **806** (1996), 28-41. (MR 98b:05098)
- (With H. Lefmann) *Canonical partition relations for  $(m,p,c)$ -systems*, Discrete Math. **162** (1996), 151-174. (MR 98a:05150)
- (With V. Bergelson, P. Erdős, and T. Łuczak) *Dense difference sets and their combinatorial structure*, in The Mathematics of Paul Erdős, I, R. Graham and J. Nešetřil, eds., Springer, Berlin, (1997), 165-175. (MR 97i:11007)
- (With W. Deuber, D. Gunderson, and D. Strauss) *Independent finite sums for  $K_m$ -free graphs*, J. Comb. Theory (Series A) **78** (1997), 171-198. (MR 98d:05140)
- (With V. Bergelson and B. Weiss) *All-sums sets in  $(0, 1]$  – Category and measure*, Mathematika **44** (1997), 61-87. (MR 98m:03099)
- (With D. Strauss) *An algebraic proof of Deuber's Theorem*, Comb. Prob. and Comp. **7** (1998), 167-180. (MR 99g:05177)
- (With I. Protasov and D. Strauss) *Strongly summable ultrafilters on abelian groups*, Matem. Studii **10** (1998), 121-132. (MR 2001d:22003)
- (With I. Leader) *Partition regular inequalities*, European J. Comb. **19** (1998), 573-578. (MR 99g:05178)
- (With V. Bergelson and R. McCutcheon) *Notions of size and combinatorial properties of quotient sets in semigroups*, Topology Proceedings **23** (1998), 23-60. (MR 2001a:20114)
- (With I. Protasov and D. Strauss) *Topologies on  $S$  determined by idempotents in  $\beta S$* , Topology Proceedings **23** (1998), 155-190. (MR 2001j:54048)
- (With V. Bergelson and I. Leader) *Additive and multiplicative Ramsey Theory in the reals and the rationals*, J. Comb. Theory (Series A) **85** (1999), 41-68. (MR 99m:05159)
- (With I. Leader) *The semigroup of ultrafilters near 0*, Semigroup Forum **59** (1999), 33-55. (MR 2002h:22004)

(With S. García-Ferreira and D. Strauss) *Orderings of the Stone-Čech remainder of a discrete semigroup*, *Topology and its Applications* **97** (1999), 127-148. (MR 2000j:54027)

(With R. McCutcheon) *Weak VIP systems in commutative semigroups*, *Topology Proceedings* **24** (1999), 199-221. (MR 2002k:20108)

(With A. Maleki and D. Strauss) *Linear equations in the Stone-Čech compactification of  $\mathbb{N}$* , *Integers* **0** (2000), #A02, 1-20. (MR 2001i:54020)

(With D. Davenport, I. Leader, and D. Strauss) *Continuous homomorphisms on  $\beta\mathbb{N}$  and Ramsey Theory*, *New York J. Math.* **6** (2000), 73-86. (MR 2001a:05148)

(With D. Strauss) *Infinite partition regular matrices, II – extending the finite results*, *Topology Proceedings* **25** (2000), 217-255. (MR 2003j:05124)

(With V. Bergelson) *Partition regular structures contained in large sets are abundant*, *J. Comb. Theory (Series A)* **93** (2001), 18-36. (MR 2002i:05116)

*Problems and new results in the algebra of  $\beta S$  and Ramsey Theory*, in Unsolved problems on mathematics for the 21<sup>st</sup> Century, J. Abe and S. Tanaka, eds., IOS Press, Amsterdam (2001), 295-305. (MR 2004a:22003)

(With R. McCutcheon) *VIP systems in partial semigroups*, *Discrete Math.* **240** (2001), 45-70. (MR 2003b:20085)

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(With R. McCutcheon) *One Sided Ideals and Carlson's Theorem*, *Proc. Amer. Math. Soc.* **130** (2002), 2559-2567. (MR 2003e:05136)

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(With D. Strauss) *Recent progress in the topological theory of semigroups and the algebra of  $\beta S$* , in Recent Progress in General Topology, II, M. Husek and J. van Mill, eds., Elsevier, Amsterdam, (2002), 227-251. (MR 1970000)

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(With D. Strauss and Y. Zelenyuk) *Large rectangular semigroups in Stone-Čech compactifications* *Trans. Amer. Math. Soc.* **355** (2003), 2795-2812. (MR 2004g:22001)

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- (With J. Pym and D. Strauss) *Multiplications in additive compactifications of  $\mathbb{N}$  and  $\mathbb{Z}$* , *Topology and its Applications*, **131** (2003), 149-176. (MR 2004d:22003)
- (With I. Leader and D. Strauss) *Separating Milliken-Taylor systems with negative entries*, *Proc. Edinburgh Math. Soc.* **46** (2003), 45-61. (MR 2004a:05155)
- (With I. Leader and D. Strauss) *Open problems in partition regularity* *Comb. Prob. and Comp.* **12** (2003), 571-583. (MR 2005e:05147)
- (With R. Kopperman) *Order compactifications of discrete semigroups*, *Topology Proceedings* **27** (2003), 479-496. (MR 2005d:05148)
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- Algebra in the Stone-Ćech compactification and its applications to Ramsey Theory*, *Sci. Math. Jpn.* **62** (2005), 321-329. (MR 2007e:54033)
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- (With M. Beiglböck, V. Bergelson, and D. Strauss) *Multiplicative structures in additively large sets*, *J. Comb. Theory (Series A)* **113** (2006), 1219-1242. (MR 2007f: 05174)
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(With L. Jones and D. Strauss), *The relationships among many notions of largeness for subsets of a semigroup*, *Semigroup Forum*, to appear. (Accepted 3/5/18)

*A history of central sets*, *Ergodic Theory and Dynamical Systems*, to appear. (Accepted 4/19/18)

(With D. Strauss), *Image partition regularity of matrices over commutative semigroups*, *Topology and its Applications*, to appear. (Accepted 7/10/18)

#### **TEXTBOOK:**

(With C. Gordon) *Elementary set theory – proof techniques*, Hafner Press, New York, 1975.

#### **RESEARCH MONOGRAPHS:**

(With D. Strauss) *Algebra in the Stone-Čech compactification – theory and applications*, Walter de Gruyter & Co., Berlin, 1998. (MR 99j:54001; Also reviewed: *Semigroup Forum* **59** (1999), 310-314.)

(With D. Strauss) *Algebra in the Stone-Čech compactification – theory and applications, second revised and extended edition*, Walter de Gruyter & Co., Berlin, 2012.

## GRANTS ADMINISTERED:

*Combinatorics: partition theory and refining families*, National Science Foundation, MCS 7606995. June 1, 1976 – November 30, 1977.

*Partition theory: sums, products, and ultrafilters*, National Science Foundation, MCS 7802330. July 1, 1978 – December 31, 1980.

*Ultrafilters and combinatorial partition theory*, National Science Foundation, MCS 8100733. June 1, 1981 – November 30, 1984.

*Ultrafilter combinatorics: Ramsey Theory and semigroups*, National Science Foundation, DMS 8320383 and DMS 8520873. June 1, 1984 – November 30, 1988.

*Combinatorics: ultrafilters, semigroups, and Ramsey Theory*, National Science Foundation, DMS 8901058 and DMS 9025025. June 1, 1989 – May 31, 1995.

*Ramsey Theory, the theory of compact left topological semigroups, and their interactions*, National Science Foundation, DMS 9424421. June 1, 1995 – May 31, 1998.

*Semigroup algebra at infinity and its combinatorial applications*, National Science Foundation, DMS 0070593 and DMS 0243586. July 1, 2000 – June 30, 2006.

*Algebra in Stone-Čech compactifications and its combinatorial applications*, National Science Foundation, DMS-0554803 and DMS-0852512. July 1, 2006 – June 30, 2012.

*Ramsey Theory: Central sets and related combinatorially rich sets*, National Science Foundation, DMS-1160566 and DMS-1460023. July 1, 2012 – June 30, 2015 and September 1, 2015 – June 30, 2017.

## DOCTORAL DISSERTATIONS DIRECTED:

Dennis E. Davenport, *The algebraic properties of closed semigroups of ultrafilters on a discrete semigroup*, Howard University, 1987.

Hanson M. Umoh, *The ideal of products in  $\beta S \setminus S$* , Howard University, 1987.

Amha Tume Lisan, *The ideal structure of the space of ultrafilters on a discrete semigroup*, Howard University, 1988.

Patty J. Anthony, *Ideals in the Stone-Čech compactification of noncommutative semigroups*, Howard University, 1994.

Gregory L. Smith, *Partition regularity of sums of products of natural numbers*, Howard University, 1994.

Dan Tang, *Separating sums from products in  $\mathbb{N}$* , Howard University, 1997.

Elaine Terry, *Finite sums and products in Ramsey Theory*, Howard University, 1997.

Shea D. Burns, *The existence of disjoint smallest ideals in the left continuous and right continuous structures in the Stone-Čech compactification of a semigroup*, Howard University, 2000.

- Jillian E. McLeod, *Notions of size in adequate partial semigroups*, Howard University, 2001.
- Iris Gugu Moche, *The sizes of preimages of points under the natural map from  $K(\beta(\mathbb{N} \times \mathbb{N}))$  to  $K(\beta\mathbb{N}) \times K(\beta\mathbb{N})$* , Howard University, 2002.
- Irene S. Moshesh, *Image partition regularity of affine transformations*, Howard University, 2006.
- Chase G. Adams, III, *Largeness of the set of finite sums of sequences in  $\mathbb{N}$* , Howard University, 2006.
- Lakeshia R. Legette, *Maximal groups in the Stone-Čech compactification of a discrete semigroup*, Howard University, 2008.
- Kendall Williams, *Separating Milliken-Taylor systems and variations thereof in the dyadics and the Stone-Čech compactification of  $\mathbb{N}$* , Howard University, 2010.
- John H. Johnson, *Some differences between an ideal in the Stone-Čech compactification of commutative and noncommutative semigroups*, Howard University, 2011.
- Henry Jordan, *Minimal Hales-Jewett sets*, Howard University, 2011.
- Kourtney Fulton Miller, *Continuous homomorphisms from  $\beta S$  to  $S^*$* , Howard University, 2013.
- Monique A. Peters, *Characterizing differences between the left and right operations on  $\beta S$* , Howard University, 2013.
- Dev Phulara, *A generalization of the Central Sets Theorem with applications and some additive and multiplicative Ramsey numbers*, Howard University, 2014.
- Kendra Pleasant, *Some new results in Ramsey Theory*, Howard University, 2017.