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## Curriculum Vitae

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EDUCATION: B.A. 1965 Westmar College
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Ph.D. 1969 Wesleyan University
(Dissertation On P-like spaces and their product with $P$-spaces written under the direction of W. W. Comfort.)

## PROFESSIONAL EXPERIENCE:

January 1980 - June 2017
Associate Professor and Professor, Howard University

September 1970 -December 1979

September 1969 -June 1970

Assistant Professor, Associate Professor and Professor, California State University, Los Angeles (Except September 1975 - August 1976, Visiting Associate Professor, SUNY at Binghamton)

Visiting Assistant Professor, Wesleyan University

## RESEARCH PUBLICATIONS:

(With W. Comfort and S. Negrepontis) $F^{\prime}$-spaces and their product with $P$-spaces, Pacific J. Math. 28 (1969), 489-502. (MR 39 \#3440)

On the existence of $\mathfrak{c}$-points in $\beta \mathbb{N} \backslash \mathbb{N}$, Proc. Amer. Math. Soc. 21 (1969), 277-280. (MR 39 \#922)

Minimal n-prime ideal spaces, Math. Ann. 199 (1972), 97-114. (MR 38 \#291)
The existence of certain ultrafilters on $\mathbb{N}$ and a conjecture of Graham and Rothschild, Proc. Amer. Math. Soc. 36 (1972), 341-346. (MR 46 \#7041)

Basically bounded sets and a generalized Heine-Borel Theorem, Amer. Math.
Monthly 80 (1973), 549-552. (MR 48 \#3000)
Preimages of points under the natural map from $\beta(\mathbb{N} \times \mathbb{N})$ to $\beta \mathbb{N} \times \beta \mathbb{N}$, Proc. Amer. Math. Soc. 37 (1973), 603-608. (MR 50 \#11154)
The product of F-spaces with P-spaces, Pacific J. Math. 47 (1973), 473-480. (MR 48 \#9643)

Finite sums from sequences within cells of a partition of $\mathbb{N}$, J. Comb. Theory (Series A) 17 (1974), 1-11. (MR $50 \# 2067)$
(With M. Cates) Partition theorems for subspaces of vector spaces, J. Comb. Theory (Series A) 19 (1975), 13-25. (MR $52 \# 112$ )
(With M. Cates, P. Erdős, and B. Rothschild) Partition theorems for subsets of vector spaces, J. Comb. Theory (Series A) 20 (1976), 279-291. (MR 53 \#10583)
(With W. Comfort) Refining families for ultrafilters, Math. Zeit. 149 (1976), 189199. (MR 55 \#285)

Partitions and sums of integers with repetition, J. Comb. Theory (Series A) 27 (1979), 19-32. (MR 81b:05018)

Partitions and sums and products of integers, Trans. Amer. Math. Soc. 247 (1979), 227-245. (MR 80b:10022)

Simultaneous idempotents in $\beta \mathbb{N} \backslash \mathbb{N}$ and finite sums and products in $\mathbb{N}$, Proc. Amer. Math. Soc. 77 (1979), 150-154. (MR 80f:05005)

Ultrafilters and combinatorial number theory, in Number Theory Carbondale 1979, M. Nathanson ed., Lecture Notes in Math. 751 (1979), 119-184. (MR 81m:10019)

Partitions and sums and products - two counterexamples, J. Comb. Theory (Series A) 29 (1980), 113-120. (MR 82b:05020)

Sums equal to products in $\beta \mathbb{N}$, Semigroup Forum 21 (1980), 221-255.
(MR 81m:54040)
On a conjecture of Erdős, Faber and Lovasz about n-colorings, Canadian J. Math. 33 (1981), 563-570. (MR 82j:05058)
Minimal ideals and cancellation in $\beta \mathbb{N}$, Semigroup Forum 25 (1982), 291-310. (MR 83m:22007)
On density, translates, and pairwise sums of integers, J. Comb. Theory (Series A) 33 (1982), 147-157. (MR 84b:10075)
(With P. Erdős) Enumeration of intersecting families, Discrete Math. 48 (1984), 61-65. (MR 84b:10075)

Partitions and pairwise sums and products, J. Comb. Theory (Series A) 37 (1984), 46-60. (MR 85g:05019)
(With J. Berglund) Filters and the weak almost periodic compactification of a discrete semigroup, Trans. Amer. Math. Soc. 284 (1984), 1-38. (MR 85e:22005)
(With P. Milnes) The ideal structure of $X^{X}$, Semigroup Forum 30 (1984), 41-51. (MR 85i:22004)
(With J. Pym) Free groups and semigroups in $\beta \mathbb{N}$, Semigroup Forum 30 (1984), 177-193. (MR 86c:22002)

Ramsey's Theorem for sums, products, and arithmetic progressions, J. Comb. Theory (Series A) 38 (1985), 82-83. (MR 86c:05024)
The minimal ideals of a multiplicative and additive subsemigroup of $\beta \mathbb{N}$, Semigroup Forum 32 (1985), 283-292. (MR 87g:20106)

The ideal structure of the space of $\kappa$-uniform ultrafilters on a discrete semigroup, Rocky Mountain J. Math. 16 (1986), 685-701. (MR 88d:54031)

Summable ultrafilters and finite sums, in Logic and Combinatorics, S. Simpson ed., Contemporary Mathematics 65 (1987), 263-274. (MR 88h:03070)
(With W. Deuber) Partitions and sums of (m,p,c)-sets, J. Comb. Theory (Series A) 45 (1987), 300-302. (MR 89a:05013)
(With A. Blass) On strongly summable ultrafilters and union ultrafilters, Trans. Amer. Math. Soc. 304 (1987), 83-99. (MR 88i:03080)
(With D. Davenport) Subprincipal closed ideals in $\beta \mathbb{N}$, Semigroup Forum 36 (1987), 223-245. (MR 89h:54031)

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(With P. Milnes) The $\mathcal{L} \mathcal{M C}$-compactification of a topologized semigroup, Czechoslovak Math. J. 38 (1988), 103-119. (MR 89c:22008)
(With V. Bergelson) Density versions of two generalizations of Schur's Theorem, J. Comb. Theory (Series A) 48 (1988), 32-38. (MR 90b:05017)
(With V. Bergelson) A combinatorially large cell of a partition of $\mathbb{N}$, J. Comb. Theory (Series A) 48 (1988), 39-52. (MR 89m:04003)

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(With D. Strauss) Algebra in the Stone-Čech compactification - theory and applications, second revised and extended edition, Walter de Gruyter \& Co., Berlin, 2012.

## GRANTS ADMINISTERED:

Combinatorics: partition theory and refining families, National Science Foundation, MCS 7606995. June 1, 1976 - November 30, 1977.

Partition theory: sums, products, and ultrafilters, National Science Foundation, MCS 7802330. July 1, 1978 - December 31, 1980.

Ultrafilters and combinatorial partition theory, National Science Foundation, MCS 8100733. June 1, 1981 - November 30, 1984.

Ultrafilter combinatorics: Ramsey Theory and semigroups, National Science Foundation, DMS 8320383 and DMS 8520873. June 1, 1984 - November 30, 1988.

Combinatorics: ultrafilters, semigroups, and Ramsey Theory, National Science Foundation, DMS 8901058 and DMS 9025025. June 1, 1989 - May 31, 1995.

Ramsey Theory, the theory of compact left topological semigroups, and their interactions, National Science Foundation, DMS 9424421. June 1, 1995 - May 31, 1998.

Semigroup algebra at infinity and its combinatorial applications, National Science Foundation, DMS 0070593 and DMS 0243586. July 1, 2000 - June 30, 2006.
Algebra in Stone-Čech compactifications and its combinatorial applications, National Science Foundation, DMS-0554803 and DMS-0852512. July 1, 2006 - June 30, 2012.

Ramsey Theory: Central sets and related combinatorially rich sets, National Science Foundation, DMS-1160566 and DMS-1460023. July 1, 2012 - June 30, 2015 and September 1, 2015 - June 30, 2017.

## DOCTORAL DISSERTATIONS DIRECTED:

Dennis E. Davenport, The algebraic properties of closed semigroups of ultrafilters on a discrete semigroup, Howard University, 1987.
Hanson M. Umoh, The ideal of products in $\beta S \backslash S$, Howard University, 1987.
Amha Tume Lisan, The ideal structure of the space of ultrafilters on a discrete semigroup, Howard University, 1988.

Patty J. Anthony, Ideals in the Stone-Čech compactification of noncommutative semigroups, Howard University, 1994.

Gregory L. Smith, Partition regularity of sums of products of natural numbers, Howard University, 1994.

Dan Tang, Separating sums from products in $\mathbb{N}$, Howard University, 1997.
Elaine Terry, Finite sums and products in Ramsey Theory, Howard University, 1997.

Shea D. Burns, The existence of disjoint smallest ideals in the left continuous and right continuous structures in the Stone-Čech compactification of a semigroup, Howard University, 2000.

Jillian E. McLeod, Notions of size in adequate partial semigroups, Howard University, 2001.

Iris Gugu Moche, The sizes of preimages of points under the natural map from $K(\beta(\mathbb{N} \times \mathbb{N}))$ to $K(\beta \mathbb{N}) \times K(\beta \mathbb{N})$, Howard University, 2002.

Irene S. Moshesh, Image partition regularity of affine transformations, Howard University, 2006.
Chase G. Adams, III, Largeness of the set of finite sums of sequences in $\mathbb{N}$, Howard University, 2006.

Lakeshia R. Legette, Maximal groups in the Stone-Čech compactification of a discrete semigroup, Howard University, 2008.

Kendall Williams, Separating Milliken-Taylor systems and variations theoreof in the dyadics and the Stone-Čech compactification of $\mathbb{N}$, Howard University, 2010.

John H. Johnson, Some differences between an ideal in the Stone-Čech compactification of commutative and noncommutative semigroups, Howard University, 2011.

Henry Jordan, Minimal Hales-Jewett sets, Howard University, 2011.
Kourtney Fulton Miller, Continuous homomorphisms from $\beta S$ to $S^{*}$, Howard University, 2013.

Monique A. Peters, Characterizing differences between the left and right operations on $\beta S$, Howard University, 2013.

Dev Phulara, A generalization of the Central Sets Theorem with applications and some additive and multiplicative Ramsey numbers, Howard University, 2014.

Kendra Pleasant, Some new results in Ramsey Theory, Howard University, 2017.

